

# RADAR METEOROLOGY

## Lecture 6 part 2

Christine Unal

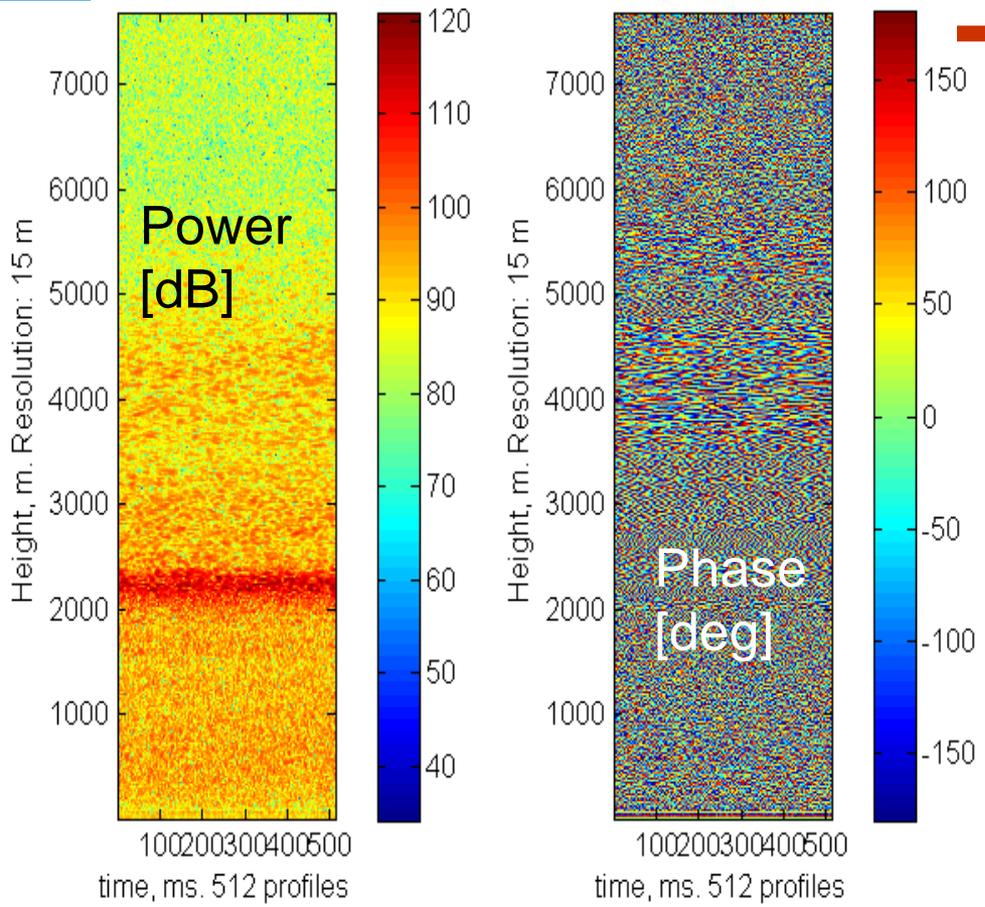


## Examples at large elevation angles

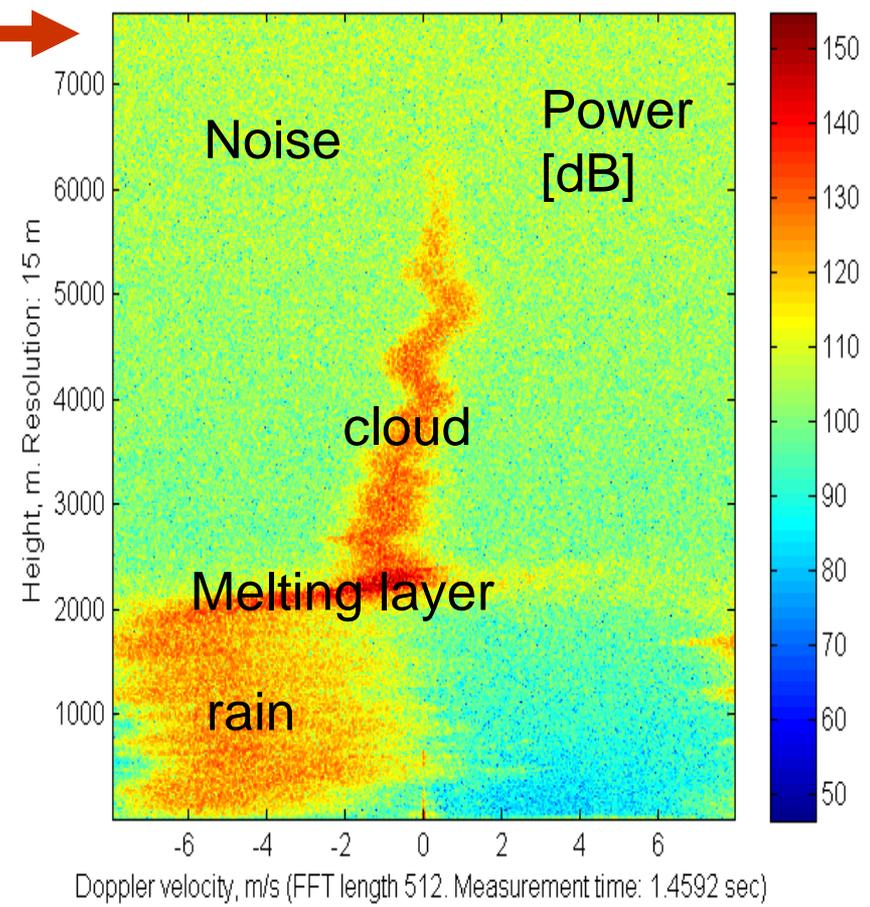


# Raw radar signal and Doppler spectra

Time series of complex signal (V) for each range bin (~s)



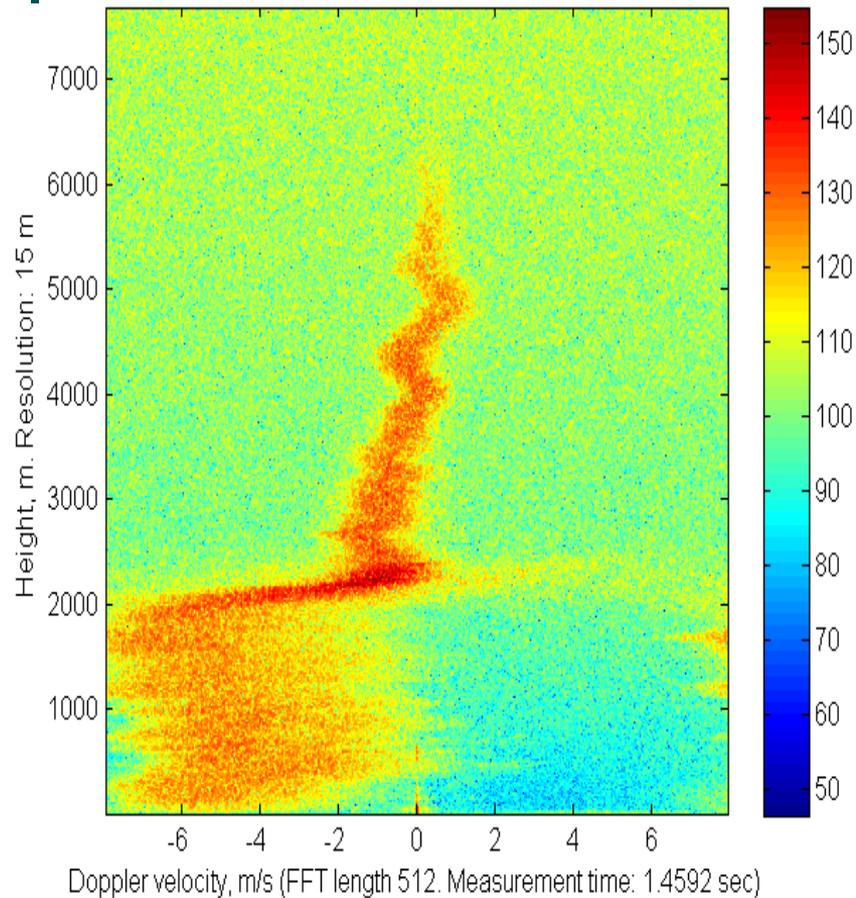
Complex Doppler spectra for each range bin: spectrogram



## Example of near-vertical profiling radar



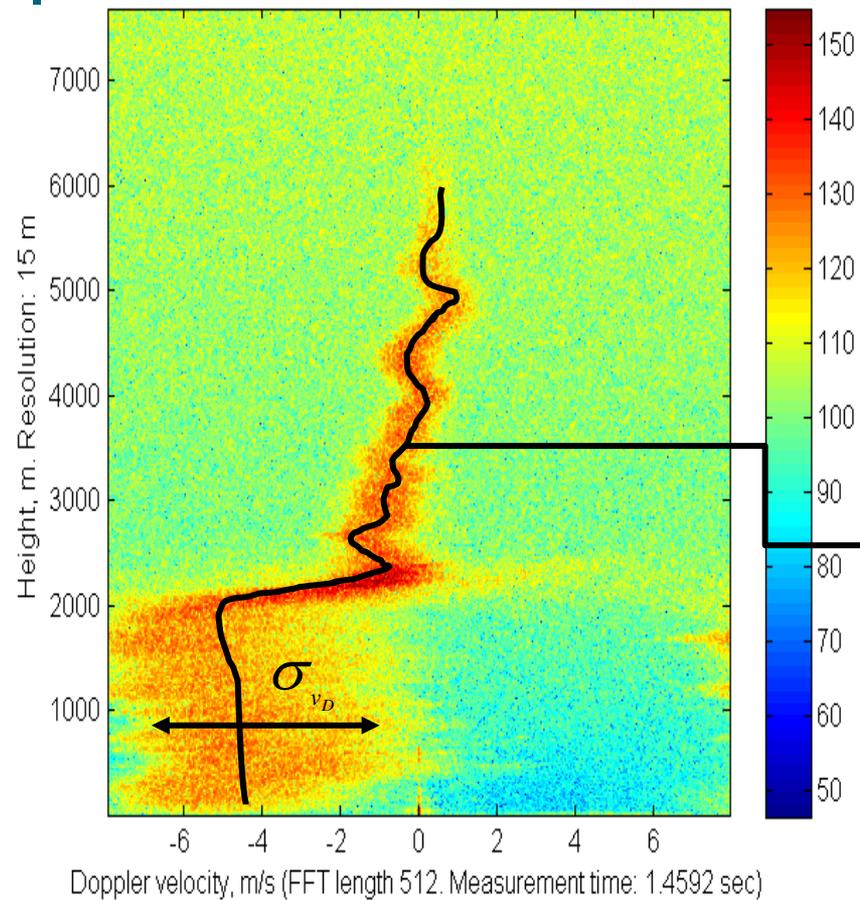
# Interpretation of the Doppler velocity



The Doppler velocity contains a large component of the fall velocity of the hydrometeors and a component of the wind (horizontal and vertical)

Example of near-vertical profiling radar ( $\alpha=75^\circ$ )

# Profiles of mean Doppler velocity and Doppler spectrum width



$$P = \int P(v)dv$$

$$v_D = \frac{1}{P} \int v P(v)dv$$

$$\sigma_{v_D} = \sqrt{\frac{1}{P} \int (v - v_D)^2 P(v)dv}$$

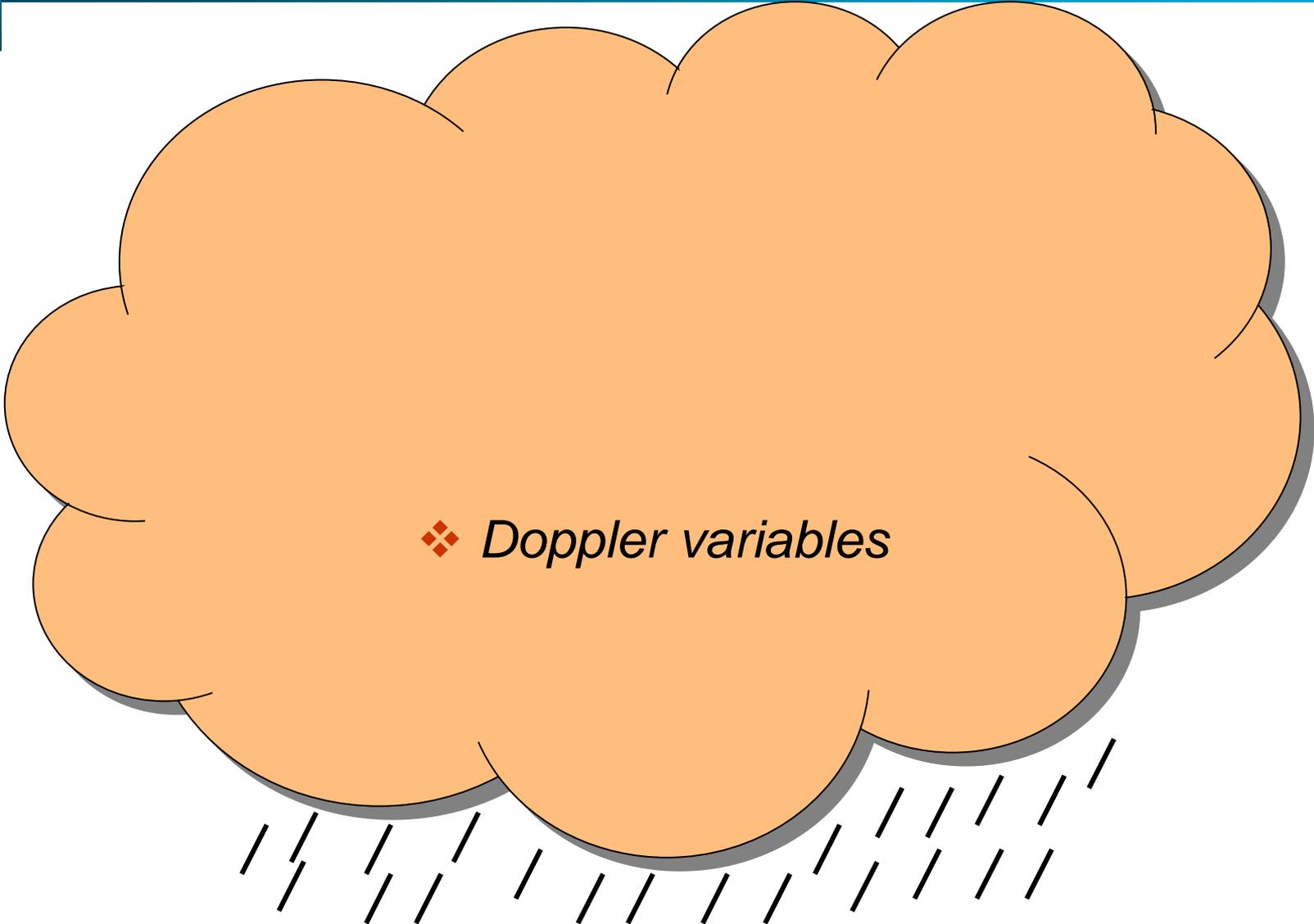
for every height

after extracting the spectrogram of hydrometeors

Example of near-vertical profiling radar ( $\alpha=75^\circ$ )

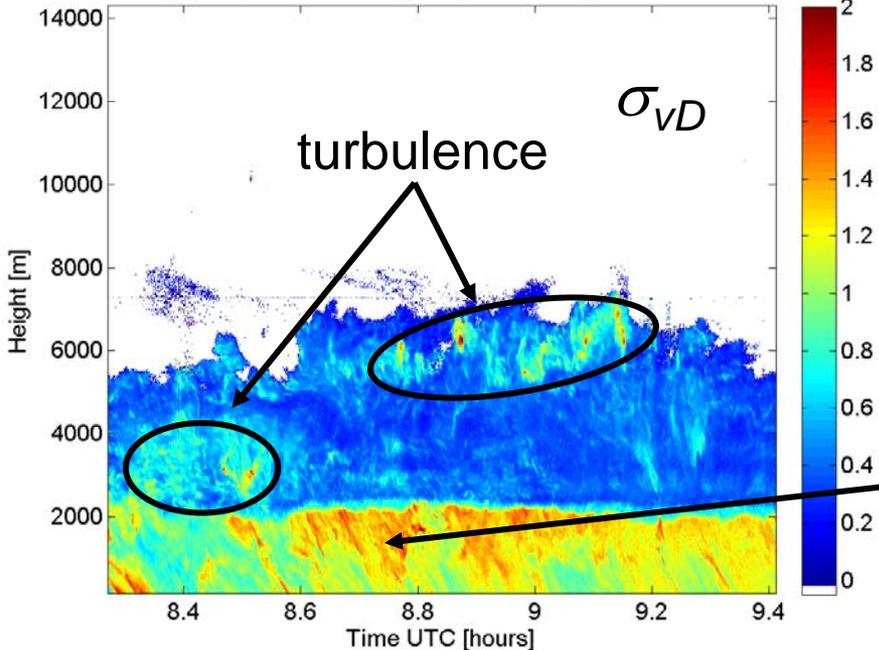
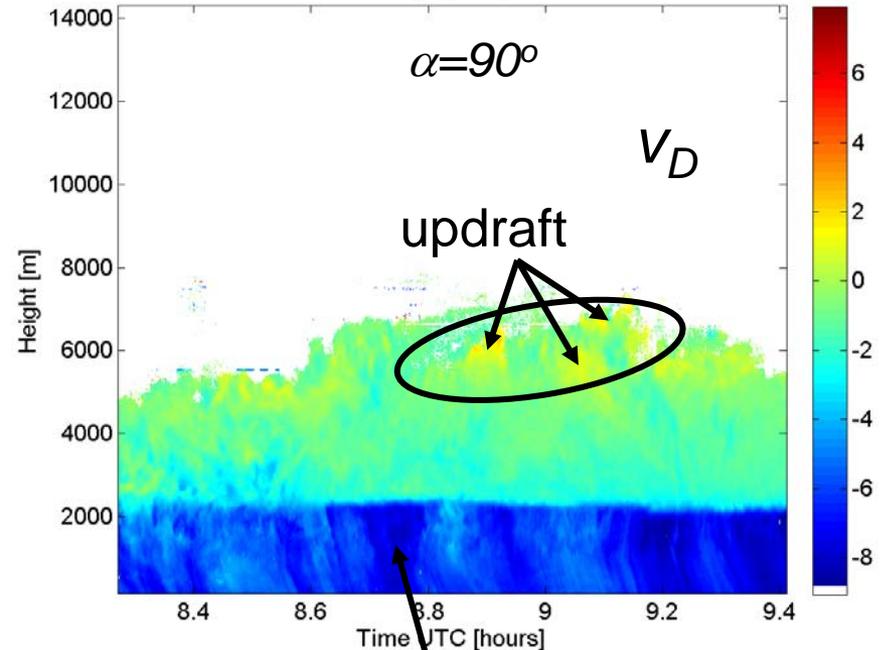
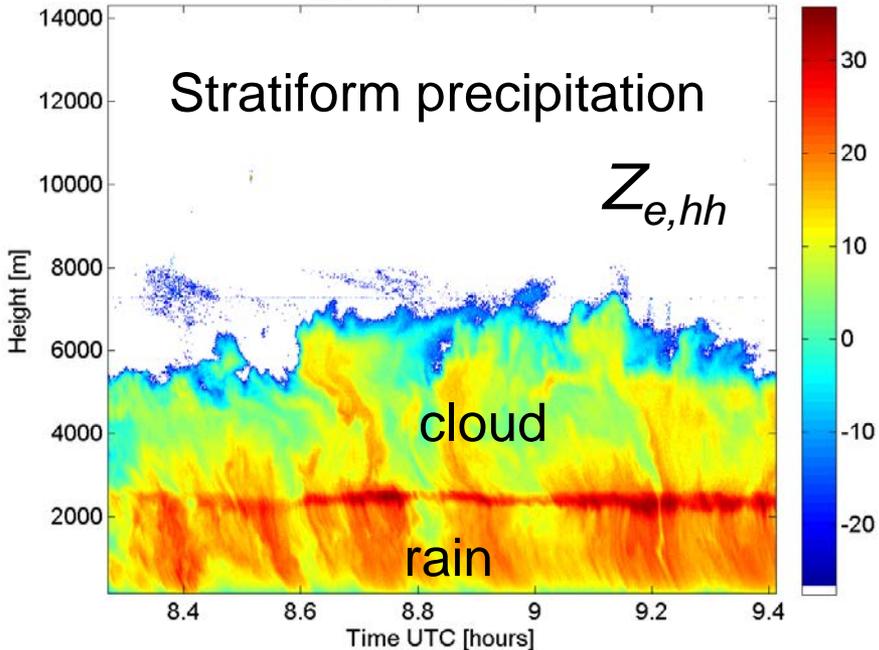


# Contents



❖ *Doppler variables*





increased fall velocity

From cloud to rain: modulus of vertical Doppler velocity and Doppler spectrum width increases (contrast). A strong vertical wind and turbulence may change this.

increased Doppler spectrum width



# Doppler variables (rain)

For an analytical expression, we need

a model for the raindrop size distribution

$$N(D) = N_0 \exp(-\Lambda D)$$

a model for the fall velocities of raindrops

$$v_f(D) = 9.65 - 10.3 \exp(-0.6D)$$

$$v_f(D) = 3.78D^{0.67} \quad \text{approximation } 0.5 < D \text{ [mm]} < 5$$



# Doppler variables (rain)

## mean Doppler velocity

$$v_D \approx - \left( \frac{\rho_0}{\rho} \right)^{0.4} \sin(\alpha) \left[ 9.65 - 10.3 \left( \frac{\Lambda}{\Lambda + 0.6} \right)^7 \right] + v_0$$

$\rho$ : air density, depends on altitude

Radar looking direction

mean fall velocity (altitude=0 m)

radial wind

“mean” droplet size

$$\langle v_f \rangle_z = \frac{1}{z} \int v_f(D) D^6 N(D) dD$$

using exponential droplet size distribution

## Doppler spectrum width

$$\sigma_{v_D} \approx \sqrt{\left( \frac{\rho_0}{\rho} \right)^{0.8} \sin^2(\alpha) \cdot (10.3)^2 \left[ \left( \frac{\Lambda}{\Lambda + 1.2} \right)^7 - \left( \frac{\Lambda}{\Lambda + 0.6} \right)^{14} \right] + \sigma_0^2}$$

turbulence

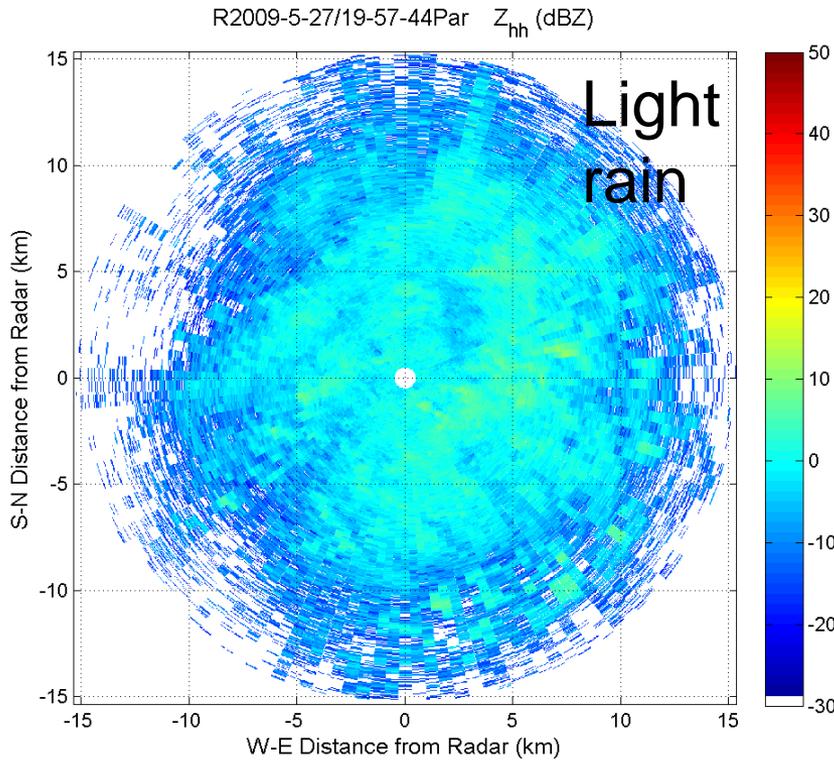


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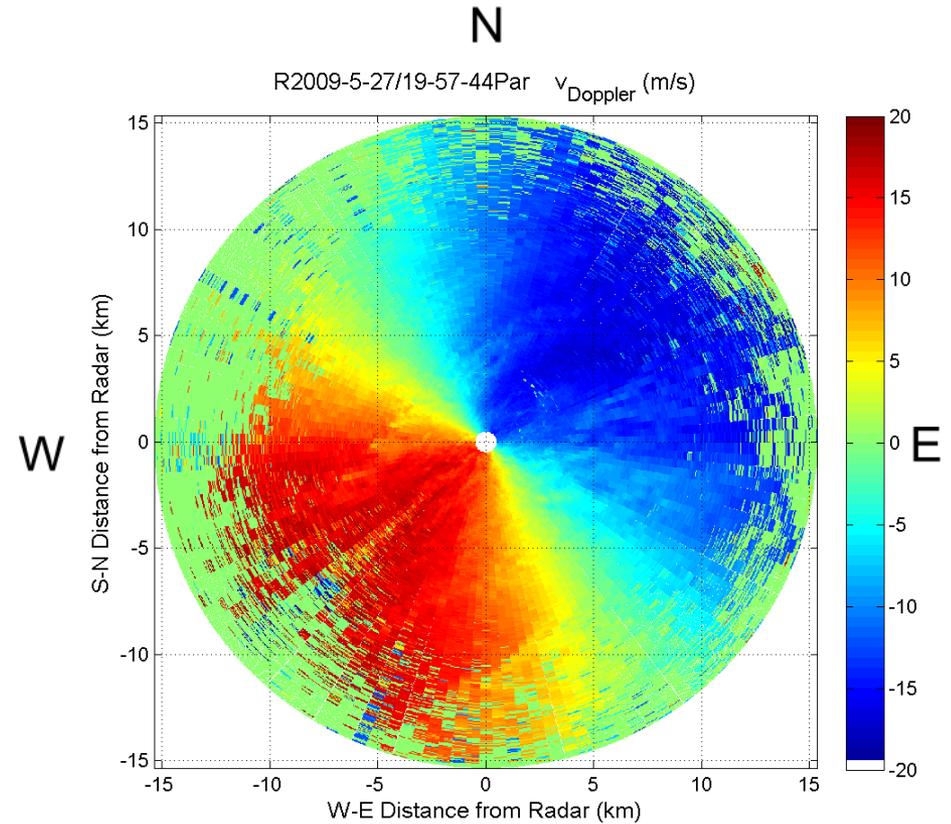
❖ *Horizontal wind estimation  
(low elevation angles)*

# Weather radar measurement example (PPI)

IDRA, Doppler-polarimetric X-band, TU-Delft



Reflectivity factor



Mean Doppler velocity

What is the wind speed and direction?

The wind direction is the direction from which comes the wind

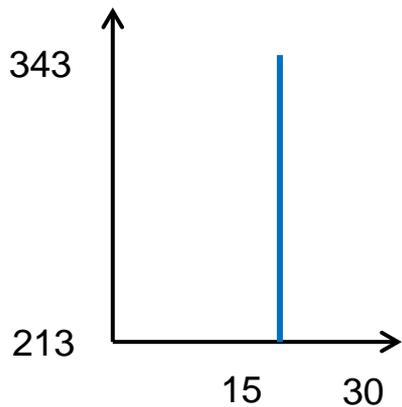


# Weather radar measurement example (PPI)

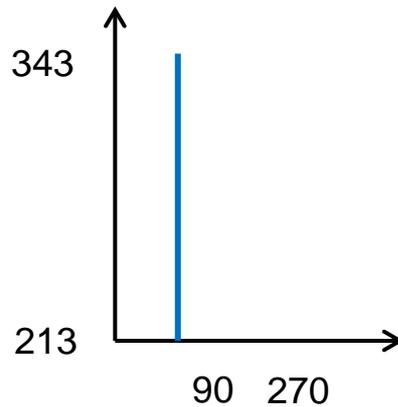
$$R_{max} = 15 \cdot 10^3 \text{ m and } \alpha = 0.5^\circ$$

$$h_{max} = 213 + R_{max} \sin(\alpha) = 343 \text{ m}$$

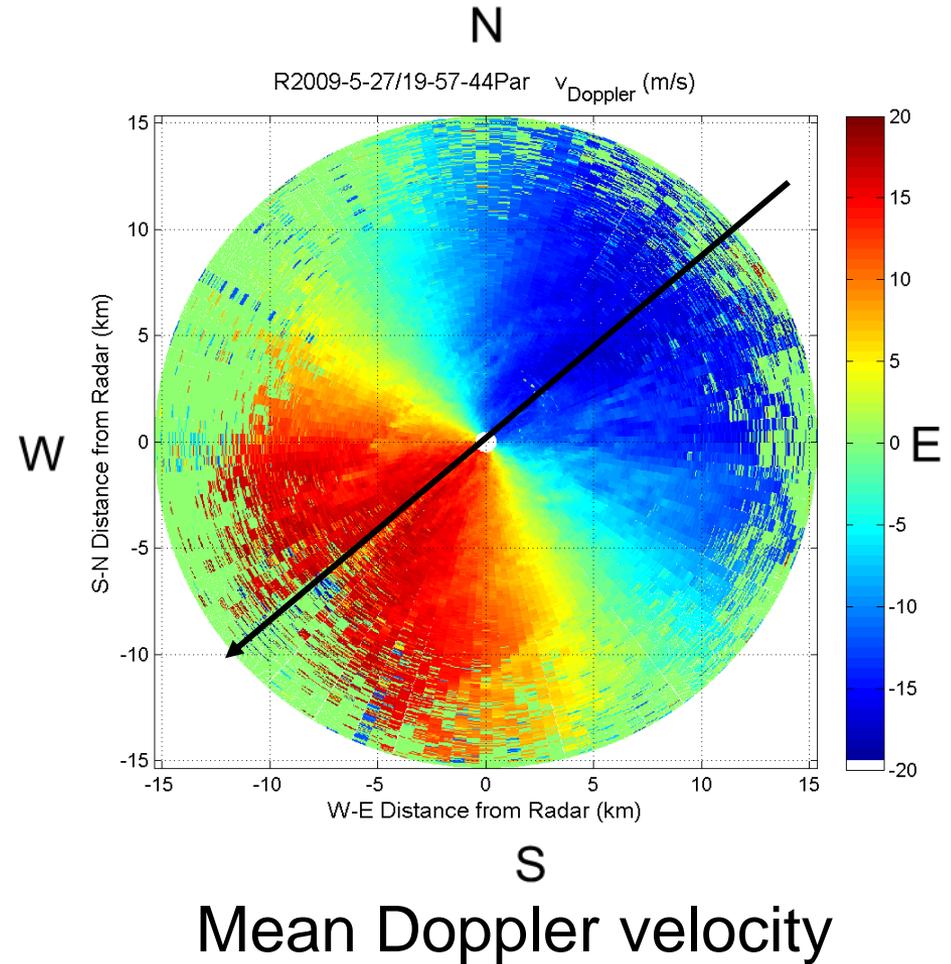
↑  
Radar placed at the top of the meteorological tower at Cabauw



Wind speed [m s<sup>-1</sup>]



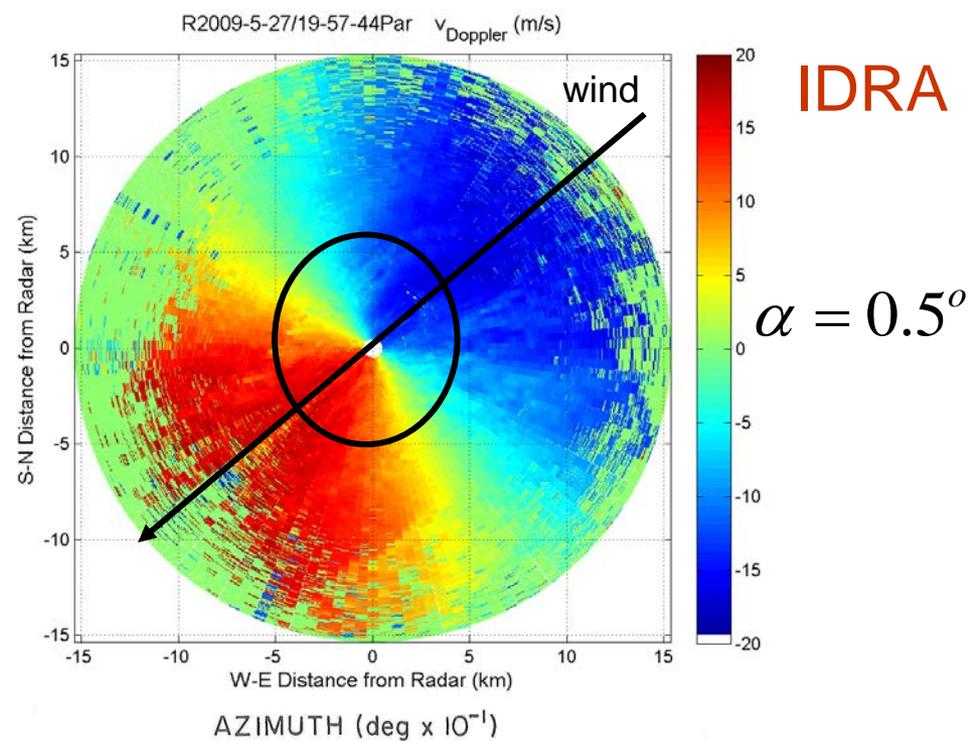
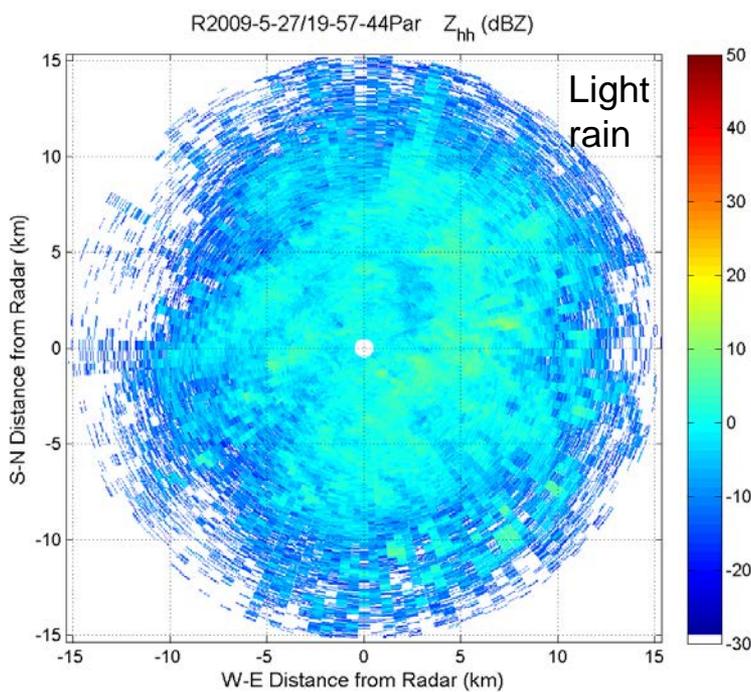
Wind direction [°]



Mean Doppler velocity

North-East wind direction with wind speed 15-20 ms<sup>-1</sup>





Horizontally  
uniform wind

At a specific height (range)

radial velocity = sine/cosine  
function of azimuth

Doviak and Zrnić, Doppler radar  
and weather observations, Fig. 9.9

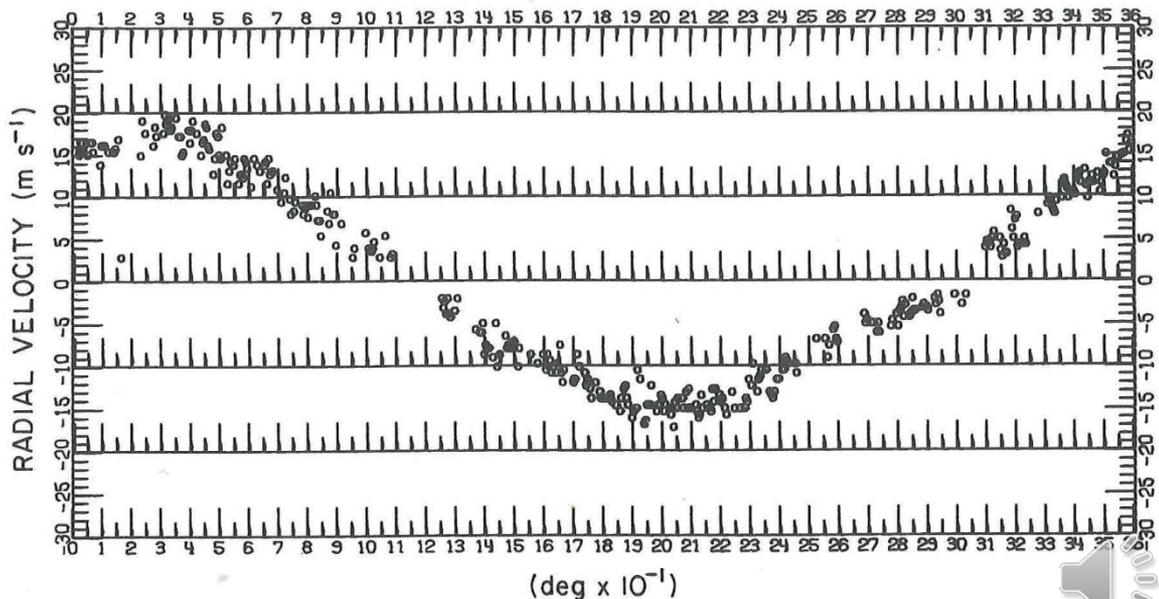


Fig. 9.9 Radial velocity at a range of 40 km versus azimuth of the Cimarron radar, 1411–1414 C.S.T., 27 April 1977. The elevation is  $0.5^\circ$ .

# Horizontal wind estimation

At a specific  
height (range)

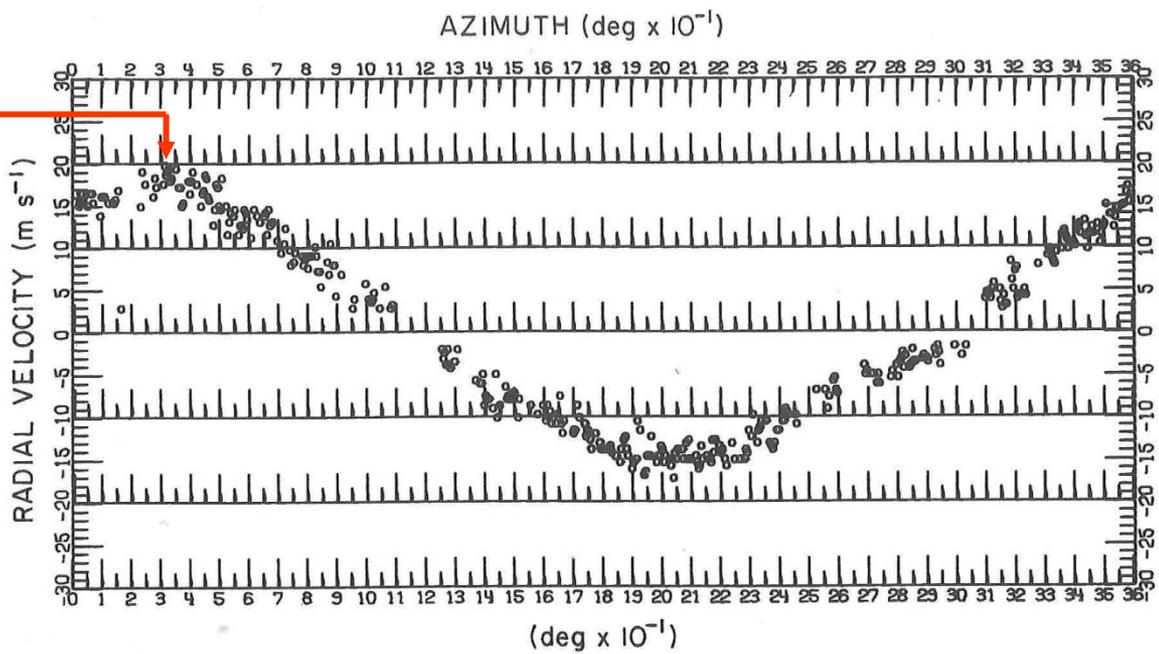


Fig. 9.9 Radial velocity at a range of 40 km versus azimuth of the Cimarron radar, 1411–1414 C.S.T., 27 April 1977. The elevation is 0.5°.

$$v_D(\phi) = \left( \cancel{w + v_f} \right) \sin \alpha + v_H \cos \alpha \cos(D - \pi - \phi)$$

velocities

$$\alpha \approx 0$$

angles

$v_D$  measured Doppler velocity

$\phi$  azimuth (related to North)

$v_H$  horizontal wind speed

$\alpha$  elevation

$w$  vertical wind velocity

$D$  horizontal wind direction (North)

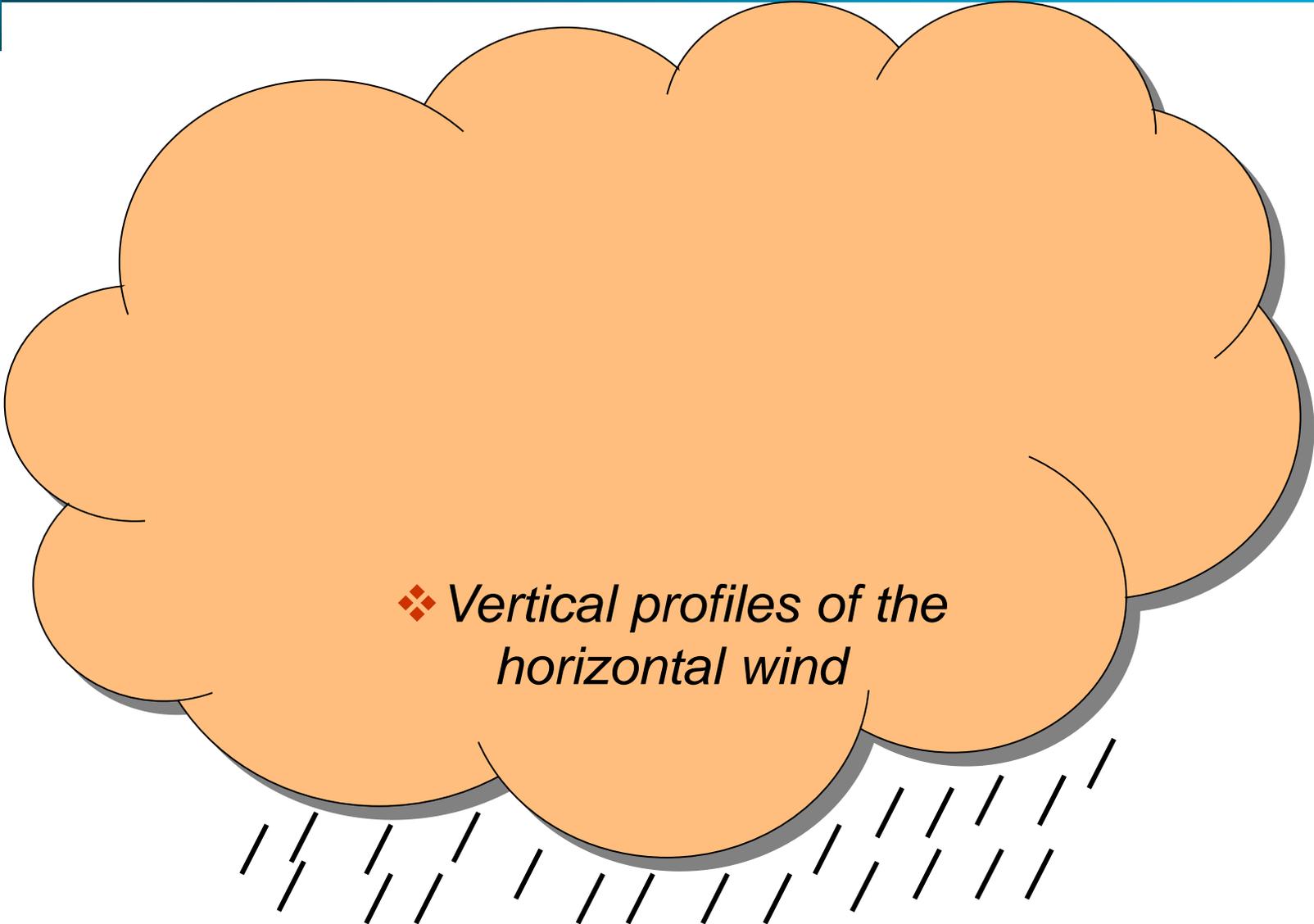
$v_f$  fall velocity



## Precipitation

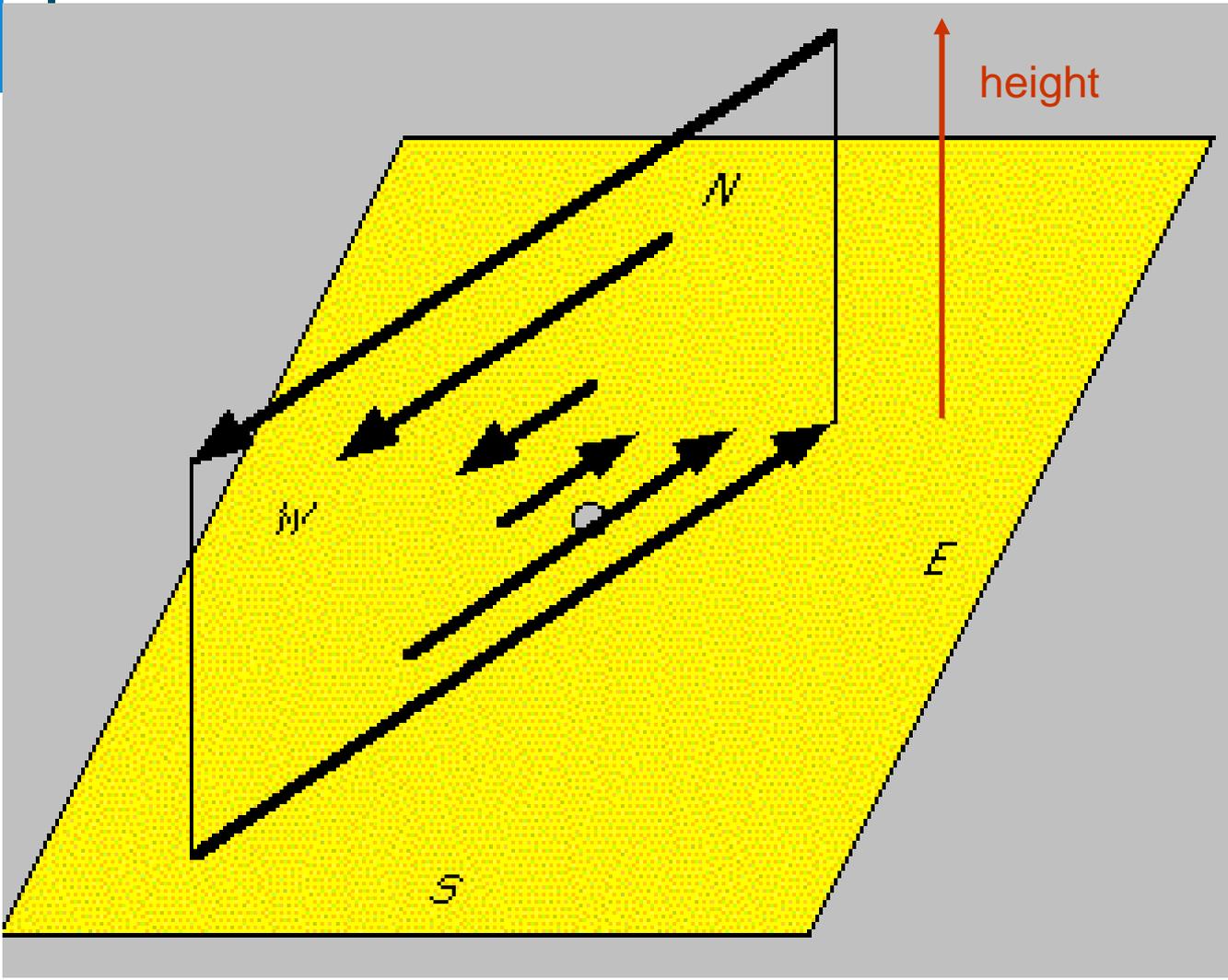
- ❖ horizontally uniform wind at fixed range
- ❖ vertical wind cannot be estimated
- ❖ the complete measurement of Doppler velocity versus azimuth is not always fully available

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❖ *Vertical profiles of the horizontal wind*

# Wind profile

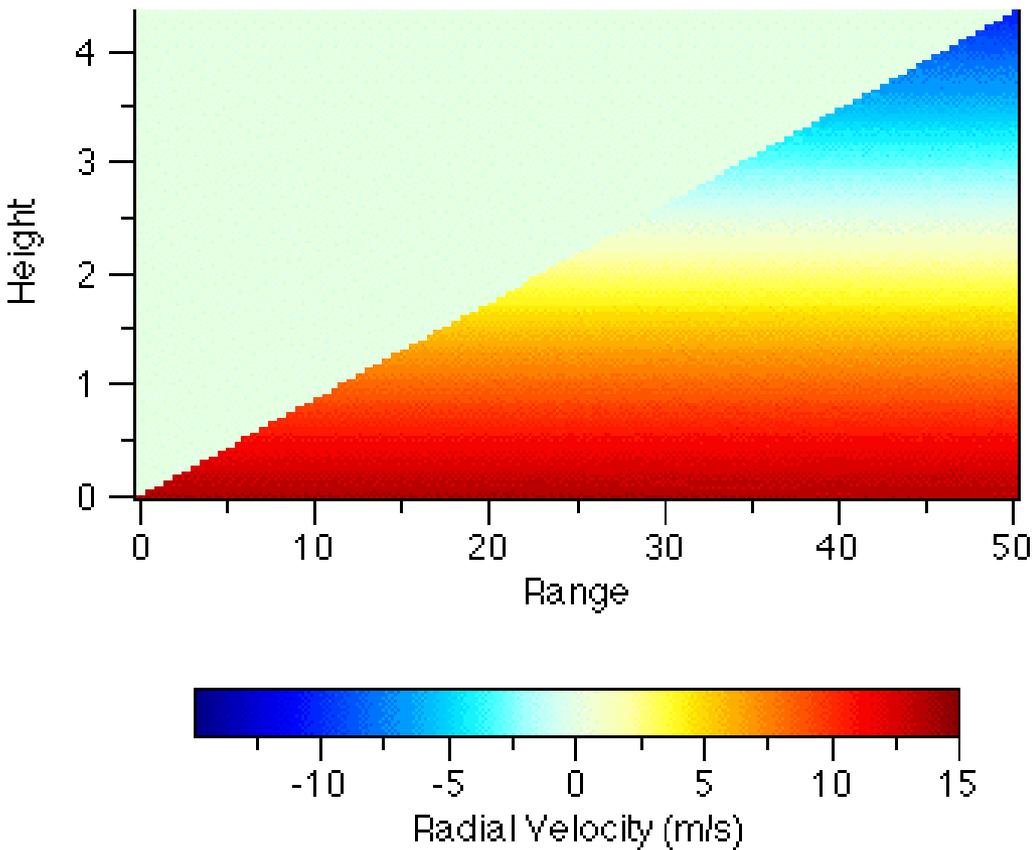


from South-West  
to North-East

Wind direction=  
direction from  
which the wind  
comes from

# Mean Doppler velocity: RHI

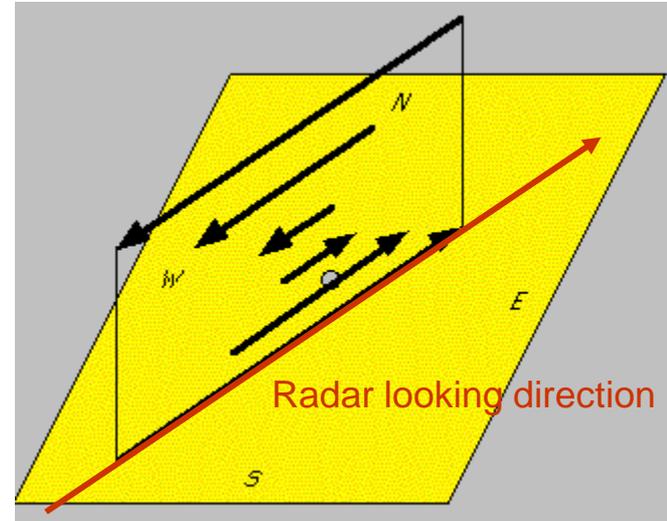
elevation scanning  $0 \leq \alpha \leq \alpha_{\max}$



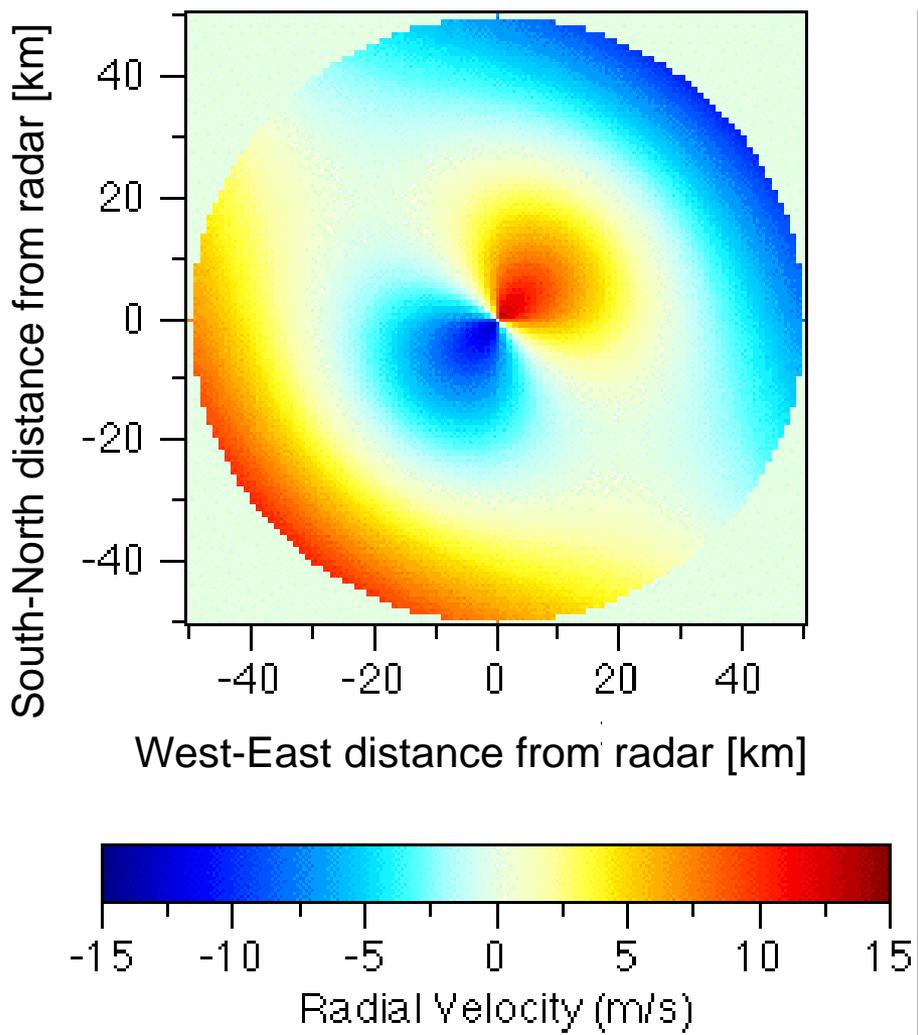
RHI

Range Height Indicator

Fall velocities: low values



# Velocity azimuth display (VAD)

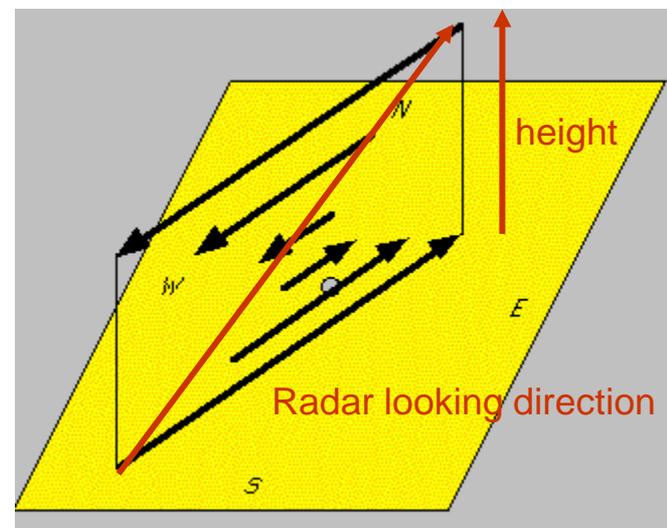


$$\alpha = \alpha_{\max}$$

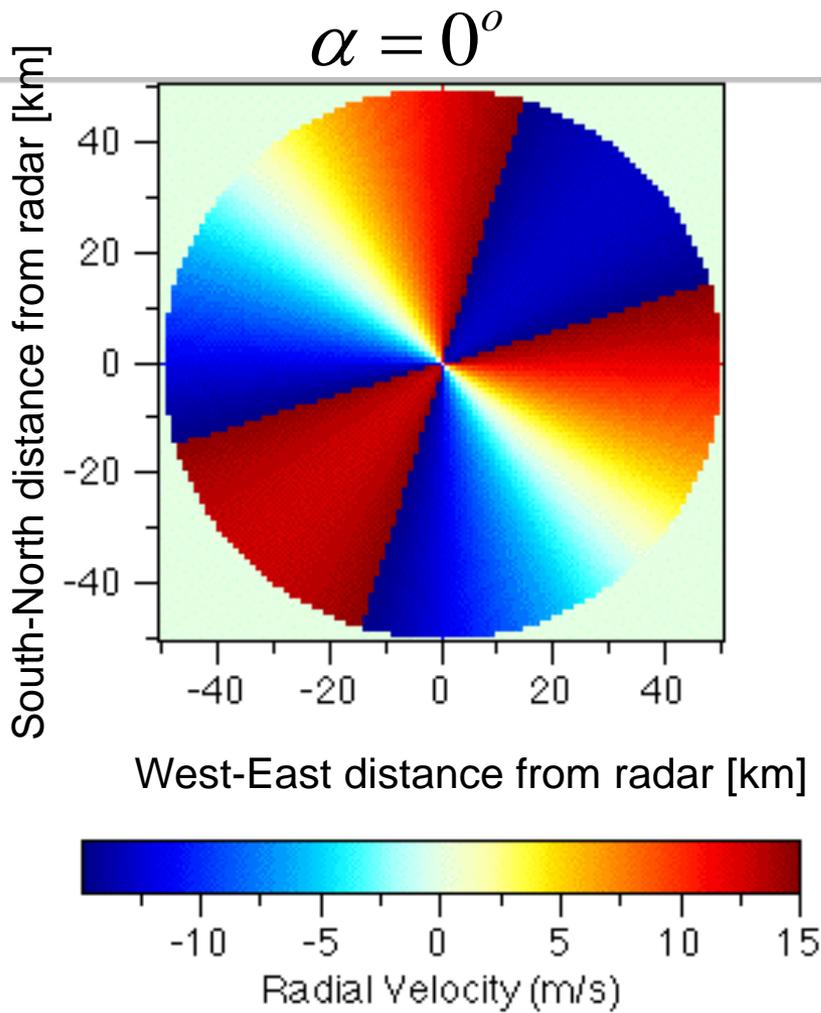
PPI

Plan Position Indicator

Fall velocities: low values

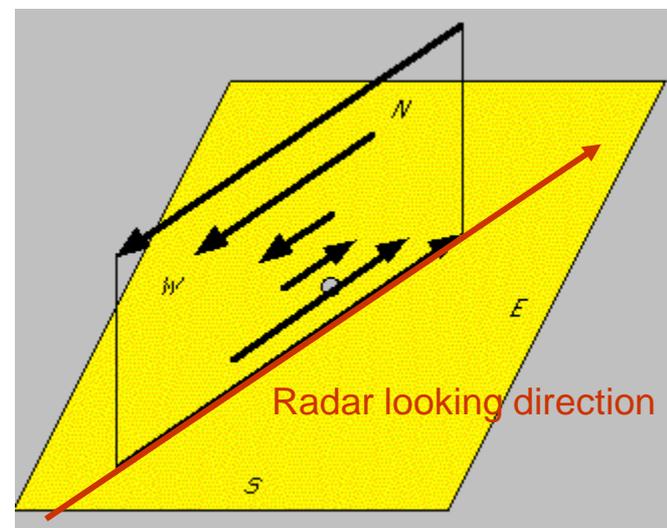


# Velocity azimuth display (VAD)

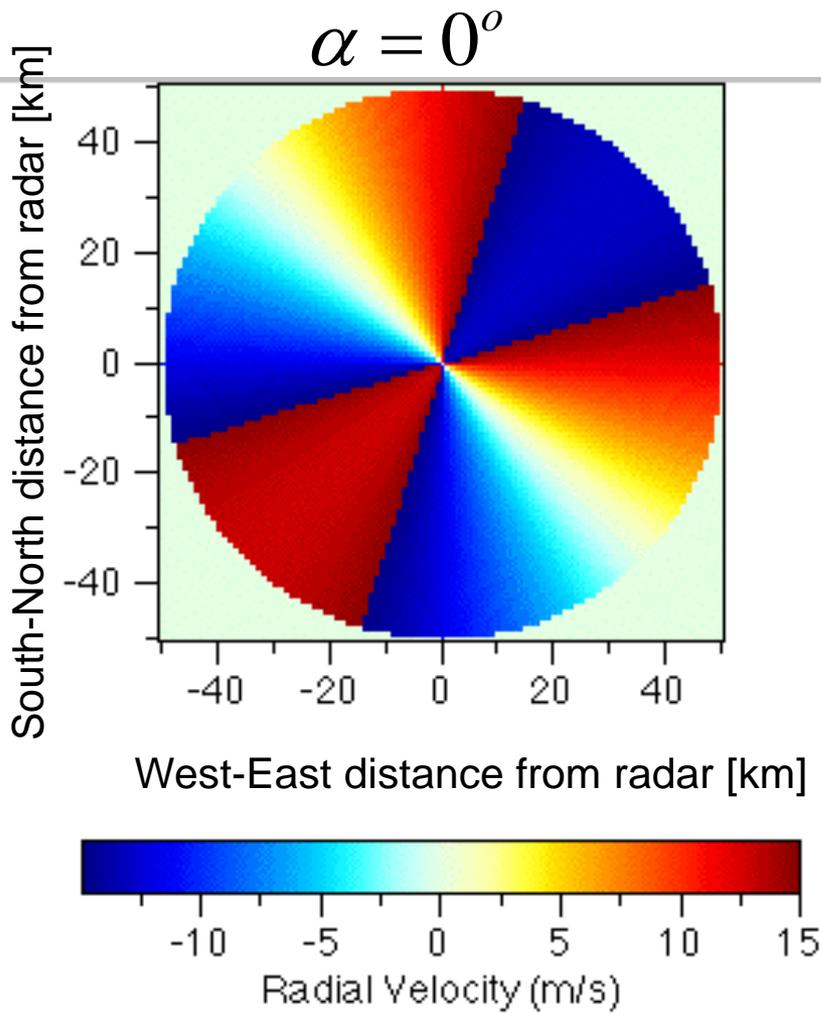


What is wrong here?

Fall velocities: low values



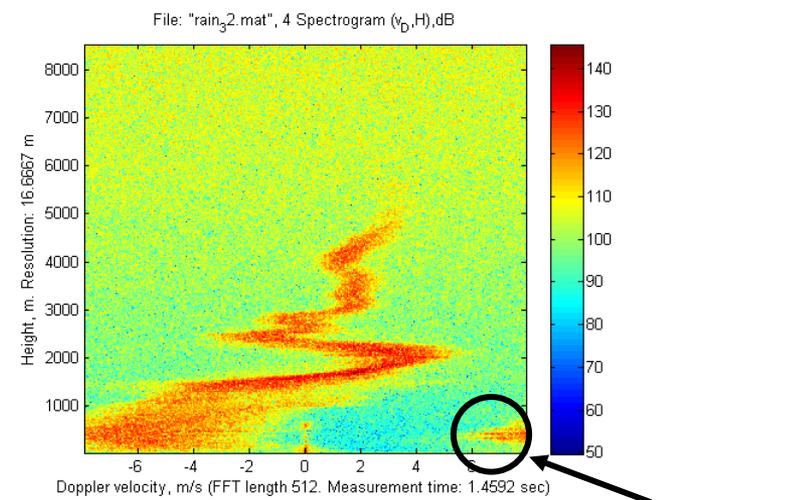
# Velocity azimuth display (VAD)



Windspeed increases

Maximum unambiguous Doppler velocity too small

$$\varphi_{\max} = \pm\pi \quad v_{\max} = \pm \frac{\lambda}{4T_0}$$



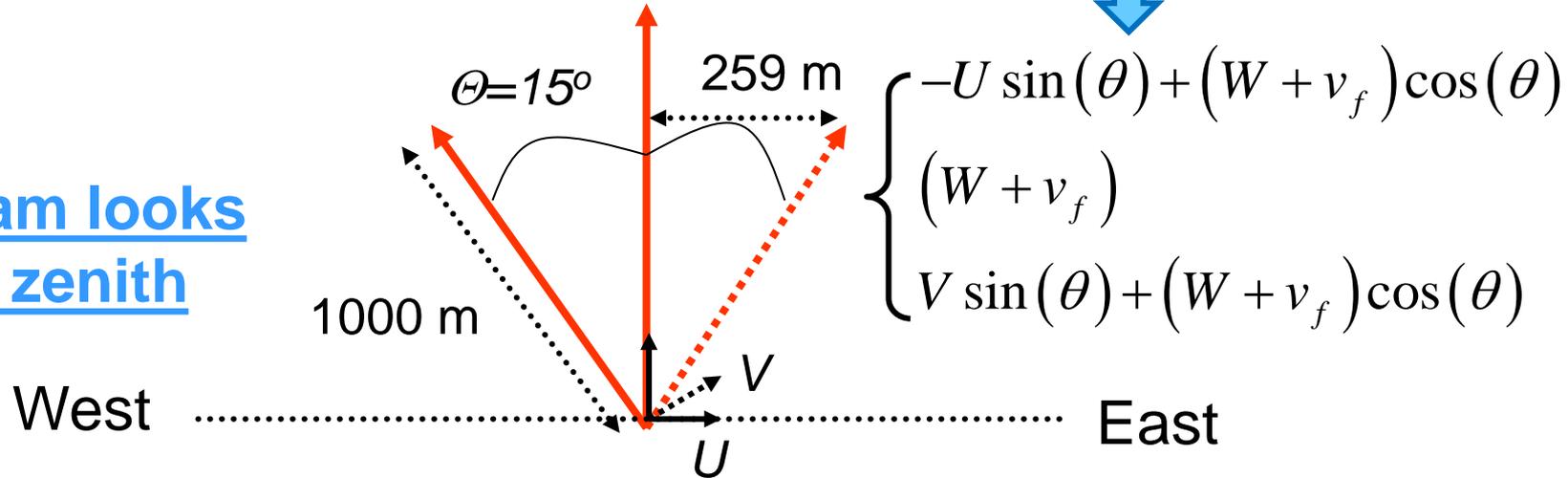
Doppler aliasing

# Radar wind profiler

a set of 3 mean Doppler velocities



One beam looks  
at the zenith



Do the measurements in three directions to obtain the  
three-dimensional wind vector  $(V, U, W)$

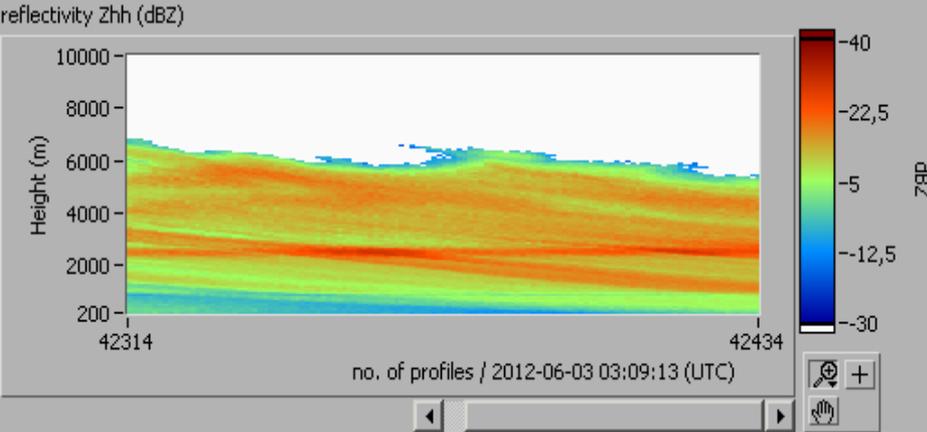
$V$ : horizontal wind component South-North

$U$ : horizontal wind component West-East

$W$ : vertical wind

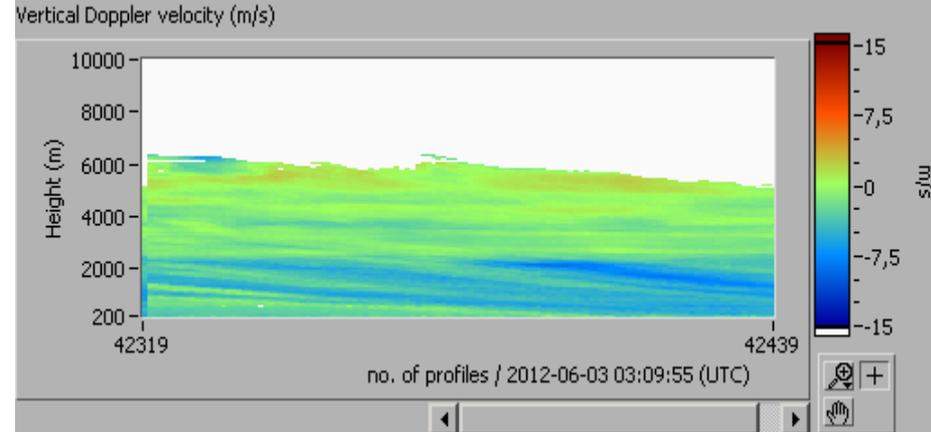
Assumption: the 3 beams probe the same medium  
(microphysical and dynamical) at fixed height





Equivalent reflectivity [dBZ]

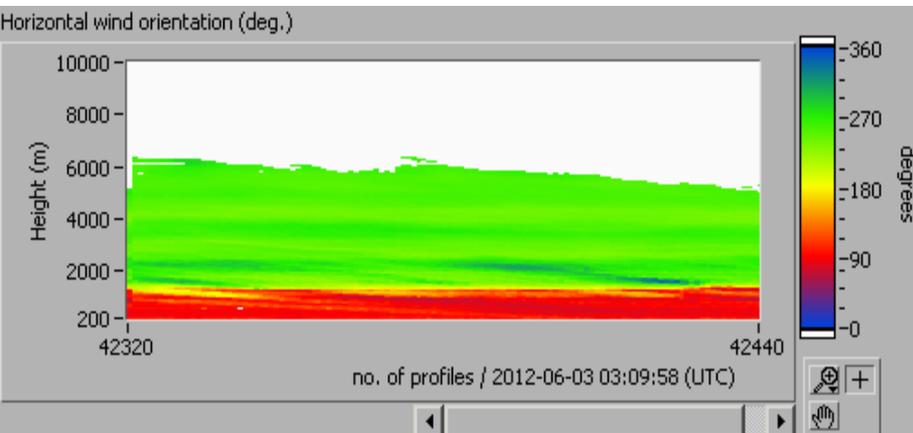
**Notice the difference of about 180 deg in wind direction**



Vertical Doppler velocity [m s<sup>-1</sup>]

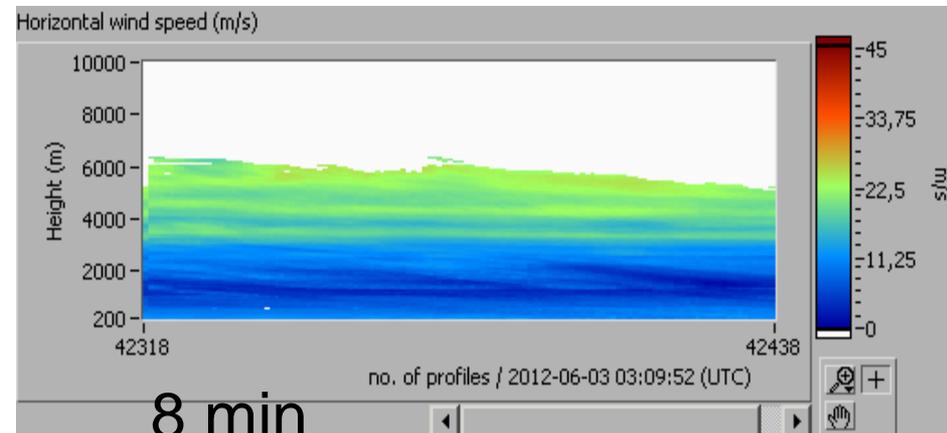
$$v_D = W + v_f$$

Elevation = 75 deg. <http://ftp.tudelft.nl/TUDELFT/irctr-rse/tara>



Horizontal wind direction [deg]

$$\tan D = \frac{U}{V}$$



8 min

Horizontal wind speed [m s<sup>-1</sup>]

$$v_H = \sqrt{U^2 + V^2}$$



## Precipitation

- ❖ 10-min averaging may suppress the contribution of turbulent effect, small time variations, Doppler velocity variance
- ❖ cannot calculate the vertical wind unless the microphysics is known (fall velocity of the particles)
- ❖ the 3 beams may probe precipitation with different microphysical properties (different fall velocities)